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SUBSTITUTE SPECIFICATION AND ABSTRACT

FLUID DENSITY MEASUREMENT IN PIPES USING ACOUSTIC PRESSURES

CROSS REFERENCES TO RELATED APPLICATIONS

This application contains subject matter related to that disclosed in U.S. Patent Applications Serial No. 09/344,094, entitled "Fluid Parameter Measurement in Pipes Using Acoustic Pressures," filed June 25, 1999; Serial No. 09/344,070, entitled "Measurement of Propagating Acoustic Waves in Compliant Pipes," filed June 25, 1999; Serial No. 09/344,069, entitled "Displacement Based Pressure Sensor Measuring Unsteady Pressure in a Pipe," filed June 25, 1999; and Serial No. 09/344,093, entitled "Non-Intrusive Fiber Optic Pressure Sensor for Measuring Unsteady Pressures within a Pipe," filed June 25, 1999, all of which are incorporated herein by reference.

TECHNICAL FIELD

This invention relates to fluid parameter measurement in pipes and more particularly to measuring speed of sound and density of fluids in pipes using acoustic pressures. The measurement exploits the interaction between pipe flexibility, speed of sound propagation, and density of the fluid within a conduit.

BACKGROUND ART

It is well known that by measuring the speed of sound (a_{mix}) of a fluid in a pipe, various parameters of the fluid may be determined, such as is described in U.S. Patent No. 4,080,837, entitled "Sonic Measurement of Flow Rate and Water Content of Oil-Water Streams," to Alexander et al.; U.S. Patent No. 5,115,670, entitled "Measurement of Fluid Properties of Two-Phase Fluids Using an Ultrasonic Meter," to Shen; and U.S. Patent 4,114,439, entitled "Apparatus for Ultrasonically Measuring Physical Parameters of Flowing Media," to Fick. Such techniques utilize a pair of acoustic transmitters/receivers (transceivers) to generate a sound signal and to measure the time it

1 takes for the sound signal to travel between the transceivers. This is also known as a
2 "sing-around" or "transit time" method. However, such techniques require precise
3 control of the acoustic source and are costly and/or complex to implement via electronics.

4 Also, these techniques use ultrasonic acoustic signals as the sound signals, which
5 are high frequency, short wavelength signals (i.e., wavelengths that are short compared to
6 the diameter of the pipe). Typical ultrasonic devices operate near 200kHz, which
7 corresponds to a wavelength of about 0.3 inches in water. In general, to allow for signal
8 propagation through the fluid in an unimpeded and thus interpretable manner, the fluid
9 should be homogeneous down to scale lengths of several times smaller than the acoustic
10 signal wavelength. Thus, the criterion for homogeneity of the fluid becomes increasingly
11 more strict with shorter wavelength signals. Consequently, inhomogeneities in the fluid,
12 such as bubbles, gas, dirt, sand, slugs, stratification, globules of liquid, and the like, will
13 reflect or scatter the transmitted ultrasonic signal. Such reflection and scattering inhibit
14 the ability of the instrument to determine the propagation velocity. For this reason, the
15 application of ultrasonic flow meters has been limited primarily to well mixed flows.

16 Gamma-densitometers are widely used in the art for performing density
17 measurements of fluids within pipes. These devices utilize a nuclear source to expose the
18 fluids to a gamma radiation beam and measure density based on gamma beam absorption.
19 The primary drawbacks of this type of density meter are the environmental and safety
20 issues associated with the nuclear sources.

21 Another prior art method of determining the density of a fluid within a pipe is
22 through the use of a Coriolis meter. A Coriolis meter measures mass flow and density as
23 the primary measurements by tracking the natural frequency of a vibrating pipe filled
24 with the fluid. These devices require a vibration source, among other elements, which
25 make Coriolis meters mechanically complex, and relatively expensive to install and
26 maintain.

27

28 SUMMARY OF THE INVENTION

29 According to the present invention, an apparatus for measuring the density of at
30 least one fluid in a pipe comprises at least two sound speed meters disposed at different
31 sensing regions along the pipe. Each sound speed meter measures an acoustic pressure

1 within the pipe at a corresponding axial location, providing an effective sound speed
2 signal indicative of the propagation velocity of a one-dimensional acoustic pressure wave
3 traveling along the pipe at each of the sound speed meters ($a_{1\text{eff}}$ and $a_{2\text{eff}}$). A signal
4 processor, responsive to the sound speed signals, provides a signal indicative of the
5 density of the fluid in the pipe.

6 According further to the present invention, the cross sectional compliance of the
7 two sensing regions is substantially different from one another. Still further, the cross
8 sectional geometry of the pipe is of a non-circular geometry in one of the two sensing
9 regions.

10 According still further to the present invention, the sound speed meters are fiber
11 optic based sound speed meters, and are isolated from an outside environment by a
12 concentric shell. The shell comprises an evacuated space, or is filled with a fluid of
13 known acoustic impedance.

14 The present invention provides a significant improvement over the prior art by
15 providing a measurement of the density ρ_{mix} of a mixture of one or more fluids within a
16 pipe (where a fluid is defined as a liquid or a gas) by using an axial array of sound speed
17 meters positioned along the pipe. An explicit acoustic noise source is not required, as the
18 background acoustic noises within the pipe (or fluid therein) will likely provide sufficient
19 excitation to enable characterization of the speed of sound of the mixture by merely
20 passive acoustic listening.

21 The invention works with acoustic signals having lower frequencies (and thus
22 longer wavelengths) than those used for ultrasonic meters, such as below about 20k Hz
23 (depending on pipe diameter). As such, the invention is more tolerant to the introduction
24 of gas, sand, slugs, or other inhomogeneities in the flow.

25 The present invention allows the density to be determined in a pipe independent
26 of pipe orientation, i.e., vertical, horizontal, or any orientation therebetween. Also, the
27 invention does not require any disruption to the flow within the pipe (e.g., an orifice or
28 venturi). Furthermore, if fiber optic sound speed meters are used to obtain the effective
29 sound speed measurements, which are well suited to the harsh down hole environment,
30 such meters eliminate the need for any electronic components down hole, thereby
31 improving reliability of the measurement.

1 Also, a strain gauge (optical, electrical, etc.) based sound speed meter that
2 measures hoop strain on the pipe may be used to measure the ac pressure. Fiber optic
3 wrapped sensors may be used as optical strain gauges to provide circumferentially
4 averaged pressure. Thus, the present invention provides non-intrusive measurements of
5 the density of the fluid, which enables real time monitoring and optimization for oil and
6 gas exploration and production.

7 The foregoing and other objects, features, and advantages of the present invention
8 will become more apparent in light of the following detailed description of exemplary
9 embodiments thereof.

10

11

BRIEF DESCRIPTION OF THE DRAWINGS

12 Fig. 1 is a schematic block diagram of a density meter, in accordance with the
13 present invention.

14 Fig. 2 is a graphical representation of the effective speed of sound of a fluid/pipe
15 system for various pipe wall thicknesses, in accordance with the present invention.

16 Fig. 3 is a graphical representation of the change in effective speed of sound of a
17 fluid/pipe system for various fluid compliances, in accordance with the present invention.

18 Fig. 4 is a schematic block diagram of a density meter having an egg shaped cross
19 section in one sensing region, in accordance with the present invention.

20 Fig. 5 is a cross sectional representation of an embodiment of a density meter
21 having a closed cell foam liner, in accordance with the present invention.

22 Fig. 6 is a schematic block diagram of a density meter having a tube positioned
23 within the flow path, in accordance with the present invention.

24 Fig. 7 is a graphical representation of the effective speed of sound of a fluid/pipe
25 system for various volume fractions of a brine/oil mixture, in accordance with the present
26 invention.

27 Fig. 8 is a schematic block diagram of a density meter having an input tube
28 positioned between the sensing regions, in accordance with the present invention.

29 Fig. 9 is a graphical representation of the effective speed of sound of a fluid/pipe
30 system for various volume fractions of a gas/fluid mixture, in accordance with the present
31 invention.

DETAILED DESCRIPTION OF THE INVENTION

3 The density meter 1 of Fig. 1 uses a pair of sound speed meters 14, 16 placed at
4 axial locations, or sensing regions, X_1 , X_2 along the pipe 12 for measuring the density of
5 at least one fluid in a pipe 12. The sound speed meters 14, 16 provide the effective speed
6 of sound $a_{1\text{eff}}$ and $a_{2\text{eff}}$ of the fluid/pipe system on lines 20, 22 which are provided to
7 signal processing logic 60 which determines the density of the fluid (or mixture) in the
8 pipe 12 using relationships between the compliance of the pipe and various fluid
9 parameters as will be more fully described below. Numerous sensing and processing
10 techniques may be employed to further determine the infinite speed of sound $a_{\text{mix}\infty}$ of the
11 fluid in the fluid/pipe system from the measured effective speed of sound a_{eff} , such as
12 those disclosed in U.S. Patent Application Serial No. 09/344,094, entitled "Fluid
13 Parameter Measurement in Pipes Using Acoustic Pressures," filed June 25, 1999, the
14 disclosure of which is incorporated herein by reference in its entirety.

15 Some or all of the functions within the logic 60 may be implemented in software
16 (using a microprocessor or computer) and/or firmware, or may be implemented using
17 analog and/or digital hardware, having sufficient memory, interfaces, and capacity to
18 perform the functions described.

19 The effective speeds of sound a_{1eff} and a_{2eff} are provided to logic 60 wherein the
20 logic calculates the density of the fluid from the difference in the effective sound speeds
21 as will be more fully described below. Sound speed meters 14, 16 utilize acoustic
22 pressure signals that, as measured, are lower frequency (and longer wavelength) signals
23 than those used for ultrasonic flow meters of the prior art, as explained in the
24 incorporated '094 application. Thus, the current invention is more tolerant to
25 inhomogeneities in the flow.

26 The typical frequency range for acoustic pressure signals of the present invention
27 is from about 10 Hz to about 10,000 Hz. The acoustic pressure signals are generated
28 within the fluid of the pipe 12 by a variety of non-discrete sources such as remote
29 machinery, pumps, valves, elbows, as well as the fluid flow itself. It is this last source,
30 the fluid flowing within the pipe, that is a generic source of acoustic noise that assures a
31 minimum level of acoustics for any fluid/pipe systems for which the present invention

1 takes unique advantage. The flow generated acoustics increase with mean flow velocity
2 and the overall noise levels (acoustic pressure levels) are a function of the generating
3 mechanism and the damping mechanism. Experience indicates that pipe systems
4 typically have sufficient ambient noise levels of 100 to 180 dbA.

5 No external discrete noise source is required within the present invention and thus
6 may operate using passive listening. It is within the scope of the present invention that
7 the sound speed meter or sensor 14, 16 spacing may be known or arbitrary and that as
8 few as two sensors are required if certain information is known about the acoustic
9 properties of the system as will be more fully described below.

10 As is known and as is described in the references incorporated herein, planar
11 compression waves 30 propagating within a fluid contained within a conduit 12 exert an
12 unsteady internal pressure loading on the conduit. The degree to which the conduit
13 displaces as a result of the unsteady pressure loading influences the speed of propagation
14 of the compression wave 30 within the fluid/pipe system. For a given fluid, the more
15 compliant the conduit, the greater the reduction of the propagation velocity of the
16 compression wave. Also, for a given pipe stiffness, the denser the fluid and the higher
17 the infinite domain sound speed, i.e., the speed of sound in an unbounded media, the
18 greater the reduction in the speed of sound due to the pipe flexibility or compliance.
19 More specifically, the relationship between the infinite domain sound speed ($a_{mix\infty}$),
20 density (ρ_{mix}) of a fluid, the elastic modulus of the pipe (E), thickness of the pipe (t), the
21 radius of a vacuum-backed cylindrical conduit (R), and the effective propagation velocity
22 (a_{eff}) for a one dimensional compression wave is given by the following expression:
23

24

$$a_{eff} = \frac{1}{\sqrt{\frac{1}{a_{mix\infty}^2} + \rho_{mix} \frac{2R}{Et}}} \quad (\text{Eq. 1})$$

25 Fig. 2 shows the effective propagation velocity, or effective sound speed for a
26 specific example of the density meter 1 of Fig. 1 in accordance with the present
27 invention. In this particular embodiment, the effective sound speed is shown for a fluid
28 contained in a vacuum-backed, cylindrical steel conduit with acoustic propagation
29 velocities and density representative of hydrocarbon liquid and water mixtures as

1 typically found in the oil and gas industry. Fig. 2 shows the effect of varying the
2 compliance of the pipe/fluid system by changing the wall thickness of a 5.50 inch OD
3 steel pipe from some theoretical minimum value to a thickness of 0.5 inches for five
4 different fluids having densities from 600 to 1000 kg/m³. As shown in Fig. 2, varying the
5 thickness of the pipe has a significant effect on the effective speed of sound of the
6 fluid/pipe system. For simplicity sake, the present invention is described with regard to
7 particular embodiments comprising vacuum-backed conduits having sufficiently low
8 frequencies (compared to breathing mode and resonant frequencies) such that the
9 pertinent dynamical response is captured by the static compliance of the conduit. The
10 conduit may be vacuum backed by a concentric shell 15 (Fig. 1) or other suitable
11 structure to isolate the sensing regions X₁, X₂ from the outside environment. In
12 alternative embodiments, the sensing regions X₁, X₂ may be isolated within the
13 concentric shell 15 by a known fluid or air. It is important that a static fluid having lower
14 acoustic impedance than the fluid flowing within the pipe surround the sound speed
15 meters. The advantages and effect of the vacuum backed conduit, as well as other
16 isolation techniques, are described in U.S. Patent Application Serial No. 09/344,070,
17 entitled "Measurement of Propagating Acoustic Waves in Compliant Pipes," filed June
18 25, 1999, which is incorporated herein by reference in its entirety.

19 Equation 1 can be generalized in terms of the cross-sectional area compliance
20 ($\sigma_{conduit}$) of the conduit and the infinite sound speed, the density of the fluid, and the
21 effective sound speed of the pipe/fluid system as given by:

22

$$\frac{1}{\rho_{eff}a_{eff}^2} = \frac{1}{\rho_{mix}a_{mix_\infty}^2} + \sigma_{conduit} \quad (\text{Eq. 2})$$

24

25 The cross sectional area compliance is a measure of the increase in cross-sectional
26 area of a conduit for a given increase in internal pressure as set forth in the following
27 relationship:

$$\sigma_{conduit} = \frac{\partial A_{cross\ section}}{\partial P} \quad (\text{Eq. 3})$$

1 For a vacuum-backed, circular cross-section pipe of elastic modulus E, having an
2 outside radius R, and wall thickness t, the conduit compliance is given by:
3

4

$$\sigma_{conduit} = \frac{2R}{Et} \quad (\text{Eq. 4})$$

5

6 It is important to note that, in general, the cross sectional area compliance of the
7 fluid/pipe system can be a complex function of frequency and amplitude and can depend
8 on all elements acoustically coupled to the conduit. For example, if an additional fluid
9 surrounded the conduit, the acoustic properties of the surrounding fluid would influence
10 the cross sectional area compliance presented to the compressional waves propagating
11 internal to the conduit. It is for this reason that the present invention is presented in
12 embodiments having a vacuum backed shell surrounding the sound speed meters as
13 described above.

14 In accordance with the present invention, using the relationships described above,
15 the dependence of propagation speed of compression disturbances (one dimensional,
16 planar compression acoustic waves) on the compliance of the conduit 12 and fluid
17 properties can be used to determine information regarding the fluid contained within the
18 conduit, specifically, the density of the fluid.

19 Referring again to Fig. 1, there is shown a density meter 1 in which the speed of
20 sound of an unknown fluid 13 is measured within two regions X₁, X₂, and in which the
21 pipe 12 has differing cross sectional area compliances associated with the two regions. A
22 first effective speed of sound a_{eff1} of the fluid/pipe system is determined from an array of
23 pressure measurements provided by sensors of sound speed meter 14. A second speed of
24 sound a_{eff2} of the fluid/pipe system is determined from an array of pressure measurements
25 provided by sensors of sound speed meter 16. As will be more fully described below, the
26 change in propagation velocity of one dimensional acoustic waves between the two
27 regions X₁, X₂, along with knowledge of the cross sectional compliances of each section,
28 provides a means to determine the density of the fluid 13. As illustrated in this example,
29 the variation in the cross sectional compliance could be achieved through a change in the
30 conduit compliance, e.g., through a change in wall thickness of the pipe. Other methods

1 to vary the cross sectional area compliance are described below, and any known method
2 of varying the cross sectional area compliance is contemplated by the present invention.

3 The invention will now be described with attention to another specific
4 embodiment commonly found in the oil and gas industry with reference to Figs. 1 and 3,
5 wherein varying the fluid compliance varies the cross sectional area compliance. In this
6 exemplary embodiment the pipe 12 is comprised of a single material type, Inconel for
7 example, have a wall thickness t_1 at region X_1 of 0.10 inches and a wall thickness of t_2 at
8 region X_2 of 0.35 inches. The pipe is vacuum backed with a shell 15 that isolates the
9 sound speed meters from the outside environment. As best shown in Fig. 3, the change in
10 sound speed for fluid mixtures, such as representative hydrocarbon and water mixtures
11 having densities ranging from 600 to 1000 kg/m³, is quite dramatic. As shown, the
12 change in sound speed scales with the acoustic impedance of the fluid. For the least
13 dense fluid with the slowest infinite medium sound speed (representing a light
14 hydrocarbon), the change in wall thickness results in approximately 300 ft/sec change in
15 sound speed. For the densest, highest infinite medium sound speed (representing, for
16 example, a high watercut mixture), the change in wall thickness results in a 750 ft/sec
17 change in sound speed. The expression for the change in effective speed of sound
18 between two sections of vacuum-backed conduits differing only in wall thickness, where
19 a_o is the speed of sound of the fluid and ρ_o is the density of the fluid is given by:

20

21

$$a_{eff_1} - a_{eff_2} = \frac{1}{\sqrt{\frac{1}{a_o^2} + \rho_o \frac{2R}{Et_1}}} - \frac{1}{\sqrt{\frac{1}{a_o^2} + \rho_o \frac{2R}{Et_2}}} \quad (\text{Eq. 5})$$

22

23 In accordance with the present invention, the density of the unknown fluid is determined
24 by measuring two effective sound speeds in two regions with differing, but known
25 structural properties. For example, in the cylindrical pipe 12 of Fig. 1, having a thickness
26 t_1 and t_2 and elastic modulus E, the density ρ_{mix} of the unknown fluid is given by:

27

1

$$\rho_{mix} = \left(\frac{1}{a_{\sigma_1}^2} - \frac{1}{a_{\sigma_2}^2} \right) \frac{E}{2R} \frac{t_1 t_2}{t_2 - t_1} \quad (\text{Eq. 6})$$

2

3 As noted above, varying wall thickness is but one way to achieve a change in
4 cross sectional area compliance, and accordingly to measure fluid density in accordance
5 with the present invention. In general, the larger the change in cross sectional area
6 compliance between the two (or more) regions in which the sound speed is measured, the
7 more robust the density measurement. In addition, an increase in the number of regions,
8 i.e. greater than two, along a pipe with varying compliance in which sound speeds are
9 measured would give additional, redundant measurements of density. The additional data
10 could yield a more robust or accurate overall system depending on the specific
11 application.

12 One alternative method to achieve large variations in conduit compliance is best
13 shown with reference to Fig. 4 where a first sensing region X_1 comprises a circular cross
14 sectional conduit while a second sensing region X_2 comprises a non-circular cross
15 sectional conduit (shown as an egg-shaped conduit by way of example). All other
16 properties of the pipe remain equal. The circular geometry at X_1 represents, for a given
17 cross section, material modulus, and wall thickness, the configuration with the lowest
18 cross sectional area compliance. However, the geometry of the cross section of the
19 modified sensing region at X_2 , formed by modifying or “egging” the circular section into
20 an oval (or other alternative shapes such as using a cross section possessing flattened
21 sides) significantly increases the compliance of the conduit 12. In certain embodiments
22 between sensing region X_2 (non-circular geometry) and sensing region X_1 (circular
23 geometry) of the same wall thickness t , cross sectional area compliance ratios greater
24 than 30 are achievable. As demonstrated above, increasing the compliance ratio of the
25 pipe section increases the sensitivity of the density calculation by increasing the change
26 in effective sound speed for a given fluid density.

27 The effective cross sectional area compliance can be modified in a variety of
28 manners such as, by way of example, by varying materials, by incorporating wall
29 treatments, or by incorporating resonators or cavities. Referring to Fig. 5, there is shown

1 a modified cross sectional area compliance technique wherein a closed cell foam 70 (or
2 other compressible liner material) is positioned along the walls of one of the sensing
3 sections of the pipe 12 to modify the effective compliance of that section of pipe. In the
4 embodiment shown in Fig. 5, the pipe/fluid interface would be defined as the inner
5 surface of the liner. An increase in fluid pressure would increase the effective cross
6 sectional area of the fluid by both compressing the foam and by expanding the pipe. It is
7 also contemplated by the present invention that the two sensing regions may be
8 comprised of different material types or any other variation in geometry or material
9 property that would effectuate a difference in the compliance of the pipe between the two
10 sensing regions.

11 In another example of the present invention, varying the compliance of the fluid
12 or the area within the pipe can vary the cross sectional area compliance. For instance,
13 and referring to Fig. 6, additional compliance could be introduced at a location along the
14 pipe by positioning a tube 72 within the flow path along one of the sensing regions. The
15 tube 72 would serve to modify the cross sectional compliance by compressing due to an
16 increase in fluid pressure, which would then combine with the compliance of the pipe to
17 modify the effective sound speed of the fluid/pipe system. Other alternatives include
18 embodiments wherein the tube is an air filled, sealed tube (or tubes) positioned within
19 one sensing region of the pipe.

20 Referring again to Fig. 1, and defining α as the ratio of conduit compliance in the
21 "soft" section (X_1) to the "stiff" section (X_2) and where σ_2 is the cross sectional area
22 compliance of sensing region X_2 , the density of the fluid ρ_{mix} within the meter can be
23 expressed as:

24

$$25 \quad \rho_{mix} = \frac{1}{(\alpha - 1)\sigma_2} \left(\frac{1}{a_{\sigma_1}^2} - \frac{1}{a_{\sigma_2}^2} \right) \quad (\text{Eq. 7})$$

26

27 Referring now to Fig. 7, there is shown the fluid sound speed of a varying mixture
28 as measured in two sensing regions X_1 , X_2 , of an embodiment of density meter 1 of Fig.
29 1. The figure shows the various effective sound speeds for oil/water mixtures varying

1 from 0% oil to 100% oil by volume. In the example shown, the two sensing sections
2 have a compliance ratio α of 10. As shown in Fig. 7, the difference in measured sound
3 speed between the two sections varies from approximately 400 m/s for 100% water, to
4 approximately 200 m/s for 100% oil. As described and depicted in the figure, the
5 effective speed of sound as measured in the stiff section (X_2) is significantly higher for
6 the mixture than that measured in the soft section (X_1) of the pipe 12.

7 In operation and referring again to Fig. 1, the two sound speed meters 14, 16
8 provide effective sound speeds $a_{1\text{eff}}$ and $a_{2\text{eff}}$ to signal processing logic 60, which includes
9 the relationship set forth in equation 7. The compliance of the conduit σ_2 in the second
10 sensing region X_2 and the ratio of the compliances between the two sections σ_1/σ_2 are
11 further provided to logic 60 to calculate the density of the mixture, ρ_{mix} . Thus the
12 density of the fluid mixture can be determined without requiring specific speed of sound
13 and calibration information concerning the fluid itself. In the embodiments described
14 thus far, it is only required that the infinite sound speed (a_{mix}) and density of the fluid
15 itself is the same in the two sections. Thus, although the density measurement described
16 is based on speed of sound measurements, no knowledge of the infinite sound speed
17 (a_{mix}) of the fluid is required to determine density.

18 In certain other embodiments, the density of the fluid may be determined after the
19 introduction of a known quantity of a known constituent into the fluid between the two
20 sensing sections. Referring to Fig. 8, there is shown a density meter 1 including an input
21 line 74 positioned between the two sensing sections X_1 , X_2 . In this particular
22 embodiment the cross sectional area compliance is changed by the introduction of a
23 constant amount of a known quantity of air 75, for example, into the fluid 13. The
24 introduction of the air into the fluid changes the cross-sectional area compliance in the
25 sensing region (X_2) downstream of input line 74. The change in compliance in the fluid
26 due to the introduction of the air is taken into account in the relationships described
27 above to accurately determine the density of the fluid 13.

28 In addition to liquid mixtures, the density meter of the present invention includes
29 the ability to determine the density of gas/liquid mixtures. Referring to Fig. 9, there is
30 shown the predicted sound speeds in the stiff (X_2) and soft (X_1) sensing regions of
31 density meter 1 of Fig. 1 for various mixtures of gas and liquids with representative

1 single phase compliances typical of produced gases and liquids at 100 bar. As shown,
2 due primarily to the high compliance of the gas phase at this relatively low pressure, the
3 change in overall sound speed in the two sections of the meter due to the change in
4 conduit compliance is much less significant for this application than those described
5 above. Using Equation 2, and by defining the compliance of the fluid as the inverse of
6 the product of the fluid density and the square of the infinite dimensional sound speed,
7 the following relation results:

8

9

$$\sigma_{mixture} \equiv \frac{1}{\rho_{mix} a_{mix_\infty}^2} \quad (\text{Eq. 8})$$

10 and the ratio of the effective sound speed within the conduit to the infinite dimensional
11 sound speed is given by:

12

$$\frac{a_{eff}}{a_{mix_\infty}} = \sqrt{\frac{1}{1 + \frac{\sigma_{conduit}}{\sigma_{mixture}}}} \quad (\text{Eq. 9})$$

13 The change in difference in sound speed for a given change in density of the fluid
14 is a useful metric in designing the density meter described for any specific application.
15 Assuming that the ratio of the cross sectional compliance introduced by the structure over
16 that of the fluid is much less than 1, this performance metric can be expressed as follows:

17

18

$$\frac{\partial(a_{1_{eff}} - a_{2_{eff}})}{\partial \rho} = \frac{a_{mix_\infty}}{\rho_{mix}} \frac{\sigma_{Stiff}}{\sigma_{mixture}} \frac{1}{2} (\alpha - 1) \quad (\text{Eq. 10})$$

19

20 As shown, effectiveness of the density meter of the present invention described scales
21 with both the ratio of the compliances of the two conduits as well as with the ratio of the
22 compliance of conduit to that of the fluid. Thus, the density meter of the present
23 invention is more effective when the cross sectional area compliance contributed by the
24 conduit is a significant fraction of that contributed by the fluid and the ratio of the cross
25 sectional area compliance of the two regions is significantly greater than one.

1 It should be understood that any of the features, characteristics, alternatives or
2 modifications described regarding a particular embodiment may also be applied, used, or
3 incorporated with any other embodiment described.

4 Although the invention has been described and illustrated with respect to
5 exemplary embodiments thereof, the foregoing and various other additions and omissions
6 may be made therein and thereto without departing from the spirit and scope of the
7 present invention.

8